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	Experiment title: Electron density studies and Accurate High Energy Diffraction experiment in zeolite LiX	Experiment number: CH-416
Beamline: ID11	Date of experiment: from: 2/04/1998 to: 8/04/1998	Date of report:
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Report:

This project on "High resolution X ray diffraction studies on dehydrated synthetic NaX zeolite" was part of the "Doctorat de l'Université H. Poincaré" ¹ of F. Porcher (defended in December 1998).

The synthetic X type zeolites, used as selective sorbants in gas separation process, exhibits a 3 dimensional framework with large (12,5 Å in diameter) supercages linked together through zigzag channels where sorbed molecules can diffuse. Their chemical composition is $M_{x/q}^{q+}(AlO_2)_x(SiO_2)_{192-x} \cdot mH_2O$ with an Si/Al ratio ranging from 1 to ~1.5.

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When this ratio is greater than 1.18, the structure is disordered and the space group is $Fd\bar{3}m$. When this ratio is close to 1, the SiO_4 and AlO_4^- tetrahedra alternate regularly in the structure and the space group can be either $Fd\bar{3}$ (total ordering of Si and Al on the tetrahedral sites) or $Fd\bar{3}m$. Si/Al influences the global negative charge of the skeleton and the location of the charge compensating cations sparse throughout the structure². Despite numerous studies, the properties of zeolites M-X, which are related to the nature of the exchangeable cations and their location within the pores, are not fully understood. Since this system is too large (~700 atoms per unit cell) for precise *ab initio* calculations, high resolution X ray diffraction is the only tool to study electron density and derive the electrostatic properties^{3,4} that govern the sorption mechanisms in the zeolite.

In this goal, we have measured high resolution X ray diffraction data sets on dehydrated NaX, ($Fd\bar{3}$ symmetry) on beamline ID11. Data collection and reduction parameters are summarized in Table 1.

Tableau 1 : Data collection parameters

Dehydrated NaX Zeolite $Fd\bar{3}$	
Chemical formula (Z=96)	$\text{Na}_{93}\text{Al}_{93}\text{Si}_{99}\text{O}_{384}$
Space group	$Fd\bar{3}$
Cell parameter	25,102(2)Å
Volume ; Density	15817(3)Å ³ , 1,425
Temperature	293 K
Radiation	$\lambda = 0,248 \text{ \AA}$
Crystal habitus	Octahedron 230 μm along [1, 0, 0]
Reflections measured	72031
$(\sin\theta/\lambda)_{\text{max}}$	1.4 Å ⁻¹
Unique reflections	6010
Reflections observed ($I > 3\sigma$)	11709
R ¹	6.96%
R ^w	5.06%

The deformation of electron density due to chemical bonding and charge transfer between atoms is modeled using Hansen-Copens model⁵ :

$$\rho_{at}(\vec{r}) = \rho_{coeur}(\vec{r}) + P_{val} \kappa^3 \rho_{val}(\kappa \cdot r) + \underbrace{\sum_l \sum_m \kappa^3 R_{nl}(\kappa \cdot r) P_{lm} Y_{lm}(\theta, \phi)}_{\delta\rho_{at}(\vec{r})}$$

with : $R_{nl}(r) = N_{nl} \cdot r^n \cdot e^{-\xi r}$

P_{lm} : multipolar populations

κ' : contraction – dilatation coefficient

$Y_{lm}(\theta, \phi)$: Real spherical harmonics.

This modeling shows (Figures 1, 2) that the maximum of the electron density is centered on the Si-O and Al-O bonds, with a slight polarisation toward neighbouring Na⁺ cations. In the hexagonal prism (Figure 1), the lone pairs of 3 oxygen atoms O2 point toward the cation Na1 they coordinate (Na1-O2 = 2.32 Å). This polarisation (Figure 2) is even more pronounced for cation Na4 which is strongly coordinated to oxygen atom O4 (Na4-O4 = 2.14 Å, Figure 3).

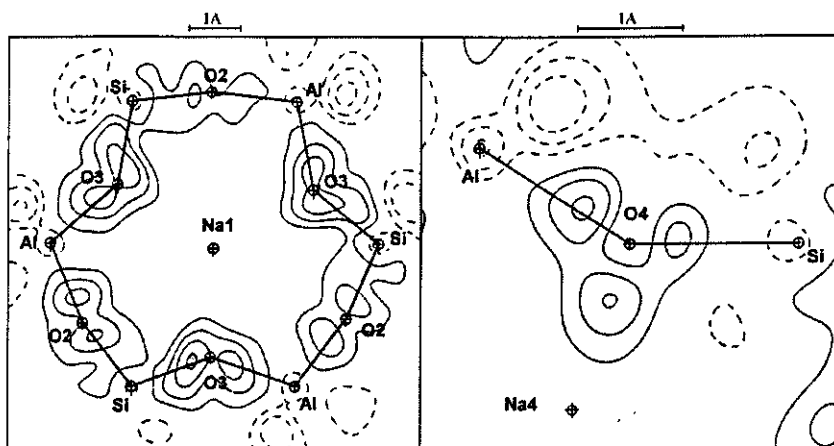


Figure 1

Figure 2

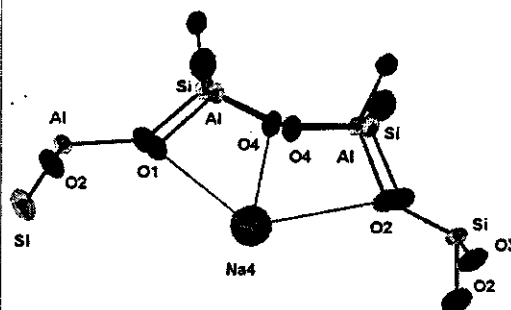


Figure 3

Dynamic deformation density in hexagonal prism (Figure 1) and Si-O4-Al plane (Figure 2) of NaX (contours : 0.1 e⁻/Å³) and coordination polyhedron of Na4(Figure 3)

The total electron density has been studied afterwards by the means of topological analysis (Bader (1991)⁶). The interactions between atoms are characterized by the topology of the electron density at its critical points, *i. e.* the points where the gradient of $\rho(\vec{r})$ vanishes:

$$\vec{\nabla}\rho(\vec{r}) = \frac{\partial\rho(\vec{r})}{\partial x_1}\vec{i} + \frac{\partial\rho(\vec{r})}{\partial x_2}\vec{j} + \frac{\partial\rho(\vec{r})}{\partial x_3}\vec{k} = \vec{0}$$

Topological analysis shows that, in the case of framework atoms, the position of the bond critical point is similar after either a spherical model or a multipolar model refinement : the critical points of Si-O and Al-O bonds sit on the bonds, as expected, and are closer to Si or Al atoms because they are more electropositive than O.

Table 2 shows that the method to position and quantify the electron density at critical point is robust in the two types of bonds (Si-O and Al-O). Electron density at critical point is higher in Si-O bonds than in Al-O ones.